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Geochemical and Magnetic Suseptibility Analysis for Critical Minerals Detection in Igneous Rocks and Beach Sand

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ABSTRACT

Critical minerals are an important natural resource that will continue to be necessary for modern industries. This study aims to determine the distribution of critical minerals based on geochemical data and magnetic susceptibility. Samples were taken from Lenggoksono beach, Southern Malang. The determination of chemical elements was conducted using X-ray fluorescence (XRF). Rare Earth Elements (REE) were identified using Inductively Coupled Plasma–Optical Emission Spectrometry (ICP-OES). Magnetic susceptibility measurements were carried out using a Barrington Magnetic Susceptibility Meter (MS2B). The results showed that the dominant elements were Silica Oxide, $SiO₂$ (70 Wt%), Iron Oxide, Fe₂O₃ (14.05) Wt%), and Calcium Oxide CaO (5.57 Wt%), which were categorized as critical minerals. The average REE elements detected were Cerium, Ce (6.75 mg/kg), Gadolinium, Gd (5.98 mg/kg), Neodymium, Nd (13.56 mg/kg), Praseodymium, Pr (6.62 mg/kg), Terbium, Tb (5.57 mg/kg), and Yttrium, Y (10.98 mg/kg). The magnetic susceptibility ranges from 13.27 to 4143.47 \times 10⁻⁸m³/kg. Pearson's Correlation analysis revealed a significant correlation between low-frequency magnetic susceptibility (χ_H) and high-frequency magnetic susceptibility (χ _{hf)} with a significance level of 0.01. χ _{If} and χ _{hf} also

showed a significant correlation with Gd, with a correlation value of $R² = 0.84$ and a significance level of 0.05. These results indicate that the presence of one critical mineral can serve as a clue to the presence of other critical minerals, and magnetic susceptibility can be used as a proxy indicator for critical minerals in natural materials.

Keywords: critical minerals, Lenggoksono, REE, magnetic susceptibility

INTRODUCTION

Modern industries continue to experience an increasing need for critical minerals in line with technological developments and climate change mitigation efforts [1-2]. The production of critical minerals is currently dominated by one country, namely China, which has 85% of the global processing capacity for Rare Earth Elements (REE) [3]. With the increasing demand for REEs, Indonesia needs to develop a sustainable resource management strategy.

As one of the countries with abundant geological resource potential, Indonesia has an excellent opportunity to contribute to meeting the global need for critical minerals. Metallic minerals such as gold, silver, copper, nickel, tin, zinc, iron, aluminum, and rare earth metals, as well as non-metallic rocks such as limestone, kaolin, zircon, phosphate, gypsum, and potassiumcontaining rocks, are some of the types of minerals found in Indonesia [4-5]. The presence of critical mineral sources can be found in igneous rocks.

Igneous rocks formed from magical activity in Lenggoksono are prime targets in the search for critical minerals. Minerals such as rare earth elements (REEs), lithium, and cobalt have an important role in various high-tech applications, including renewable energy and electronics [6-7]. However, identifying and quantifying these critical minerals is often challenging due to their uneven distribution and relatively low concentration in the host rock. When a mineral is considered important to the country's economy and security and is vulnerable to global supply risks, especially when REE production comes from limited mineral resources, it is classified as a critical mineral.

Geochemical analysis and magnetic susceptibility produce important data for detecting minerals and critical characterization in rock formations. This method involves collecting and interpreting chemical data from coastal rocks and sand samples, which can reveal patterns and anomalies associated with mineralization. With advances in analytics and data processing techniques. Modern geochemical analysis allows for the detection of critical minerals with a higher level of sensitivity and accuracy, even at very low concentrations [8-9].

This study aims to analyze the critical distribution of minerals in the Lenggoksono region. This analysis is based on igneous rock and sand samples obtained in the Lenggoksono area.

METHOD

Geographical Location and Geological Conditions of Lenggoksono

Purwodadi Village has an area of 1041 Ha, divided into three hamlets: Balaearjo, Purwodadi, and Lenggoksono. Geographically, this region is located at 8°20'0''LS-82o5'0 "S and 112°47'0''BT-112o52'0''E [10]. Based on the geological map shown in FIGURE 1, the Lenggoksono area with mandalika formations is dominated by andesite, basalt, tract, dacite and dispersed andesite breccia (Tomm) lava. Members of the Mandalika Formation Tuff which is dominated by rhyolite-dacite tuft, pumice tuff breccia (Tomi). Swamp and river deposits are dominated by gravel, sand, clay and plant residues (Qas) [11].

FIGURE 1. Geological map of Lenggoksono (Created by QGIS)

Sampling and Sample Preparation

This research was carried out in several stages, starting with a literature study on Rare Earth Elements (REE) and critical minerals. Furthermore, the identification of sampling locations in the Lenggoksono area was carried out. The sampling points are shown in detail in FIGURE 2. The sampling process can be seen in FIGURE 3(a); the samples taken are in the form of igneous rocks found in the Lenggoksono River and sand from the Lenggoksono River, Wedi Awu Beach, and Lenggoksono Rivers.

The next stage is the sample process carried out in the laboratory. Sample preparation begins with scraping the sample using mortar, as seen in FIGURE 3(b), followed by drying on a plastic plate lined with perforated plastic wrap. Next, we weigh the samples and perform Xray fluorescence (XRF) tests to identify chemical elements associated with critical minerals [12].

Measurement

In general, XRF is used to determine the constituent elements of a material. XRF analysis can be done qualitatively and quantitatively [13-14]. In addition to the XRF test, this study also uses the ICP-OES technique to analyze the content of Rare Earth Element (REE) and the magnetic susceptibility test as shown in FIGURE 3(c) is a sample that is ready for magnetic susceptibility test. Magnetic susceptibility is measured with the MS2B magnetic susceptibility meter. Magnetic susceptibility can be used to determine the indication of magnetic mineral content in nature in the presence of Fe. The magnetic susceptibility value can be used to determine the properties of magnetic minerals [15].

Meanwhile, measurements with ICP-OES begin by inserting a sample in liquid form into a nebulizer. These aerosols are then delivered to the main plasma, where the ionization of atoms and the excitation of electrons occur. When an electron returns to its base energy level, the energy is released in the form of radiation of a specific wavelength. This radiation is then detected by sensors to identify and measure the concentration of the elements in the sample [16-18]. The data then analyzed with statistical software (SPSS). This test was carried out to determine the linear relationship between one variable and another variable between critical mineral elements and REE elements, as well as magnetic susceptibility that can indicate mineral dispersion [19].

FIGURE 2. Sampling Location Point (Created by QGIS)

FIGURE 3. (a) Sampling, (b) Scraping of samples, (c) Samples ready for testing

RESULTS AND DISCUSSION

Geochemistry of Igneous Rocks

The chemical element content test results of the selected sample can be seen in TABLE 1. The composition of chemical elements showed that $SiO₂$ content was the dominant element in all samples, ranging from 55.1% by weight to 81.88% by weight $Fe₂O₃$ compounds had varying values, with the highest content of 23.1% by weight (PSL) and the lowest at 6.76% by weight (BBL 2). Al_2O_3 compounds were detected in PSL, BBL 1 and BBL 2 samples with concentrations of 12% by weight to 13% by weight CaO compounds varied from 2.6% by weight to 13% by weight with BBL 1 having the highest concentration. The full content of the compound can be seen in TABLE 1.

Rare Earth Elements (REE)

The total REE concentration ranged from 27.36 mg/kg (BBL 2) to 79.35 mg/kg (BBL 1) shown in TABLE 2. The BBL 1 sample showed the most significant REE dominance with total REE concentrations nearly tripling compared to the lowest sample, indicating mineralization potential zones of interest for further exploration [20-21]. The distribution of Light Rare Earth Elements (LREE) and Heavy Rare Earth Elements (HREE) varied between samples. LREE (Ce, Nd, Pr) is generally more dominant in most samples, except in WA 1 and BBL 2 where HREE (Gd, Tb, Y) is more prominent. The high LREE content is related to the type of host rock such as granite or granitoid rocks that are rich in LREE-carrying minerals. The dominance of LREE, especially in LGSN 1, LGSN 2, and PSL samples, is consistent with patterns commonly found in many terrestrial REE deposits [22]. However, the relatively high enrichment of HREE in some samples, especially BBL 1 and WA 1, is interesting from an economic perspective because HREE is generally rarer and of higher value [23]. The magnetic REE distribution map is shown in FIGURE 4. FIGURE 4 (a) shows the distribution of Cerium (Ce) in the Lenggoksono region, based on the map this element has the highest concentration at the LGSN 1 point with an average of 7.52 mg/kg. In the Yttrium (Y) element, the distribution map is shown in FIGURE 4 (b) where the location point with the highest average is BBL 1 of 12.94 mg/kg, indicating that at LGSN 1 and BBL 1 are potential REE zones.

| Compound | Sample Name | | | | | | |
|--------------------------------|--------------------|---------------|-------------|------------|-------|-------------|------------------|
| Oxides $(wt\%)$ | LGSN1 | LGSN 2 | WA 1 | WA2 | PSL | BBL1 | BBL ₂ |
| Al_2O_3 | 0.00 | 0.00 | 0.00 | 0.00 | 13.00 | 12.00 | 13.00 |
| SiO ₂ | 77.40 | 81.80 | 76.00 | 74.70 | 55.90 | 55.10 | 73.50 |
| SO ₃ | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 1.90 | 2.20 |
| P_2O_5 | 0.00 | 0.00 | 0.00 | 0.00 | 0.95 | 0.00 | 0.00 |
| K_2O | 1.10 | 0.84 | 0.95 | 0.90 | 1.61 | 0.48 | 0.54 |
| CaO | 2.98 | 3.62 | 7.12 | 6.98 | 2.60 | 13.00 | 2.72 |
| TiO ₂ | 1.31 | 1.40 | 2.32 | 2.11 | 1.26 | 1.15 | 0.79 |
| V_2O_5 | 0.04 | 0.03 | 0.07 | 0.08 | 0.06 | 0.07 | 0.02 |
| Cr_2O_3 | 0.04 | 0.04 | 0.05 | 0.05 | 0.06 | 0.05 | 0.03 |
| MnO | 0.28 | 0.24 | 0.20 | 0.21 | 0.49 | 0.16 | 0.17 |
| Fe ₂ O ₃ | 13.70 | 11.6 | 12.90 | 14.60 | 23.10 | 15.70 | 6.76 |
| CuO | 0.07 | 0.06 | 0.06 | 0.07 | 0.09 | 0.05 | 0.04 |
| ZnO | 0.05 | 0.03 | 0.03 | 0.00 | 0.13 | 0.00 | 0.02 |
| MoO ₃ | 2.70 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 |
| Eu ₂ O ₃ | 0.20 | 0.22 | 0.20 | 0.20 | 0.32 | 0.20 | 0.10 |
| Yb_2O_3 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.03 |
| Re ₂ O ₇ | 0.10 | 0.10 | 0.10 | 0.00 | 0.10 | 0.00 | 0.07 |

TABLE 1. Composition of Enggoksono samples measured by X-Ray Fluorescene

TABLE 2. Lenggoksono Rare Earth Element Data

| Nama | Rare Earth Element (ppm) | | | | | | LREE | HREE | Total | Tmag | Tnon |
|-------------------|--------------------------|------|-------|--------|--------|-------|-------|-------------|------------|-------|------------|
| Sampel | Ce. | Gd | Nd | Pr | Tb | Y | | | REE | | Mag |
| LGSN 1 | 11.72 | 4.15 | 14.88 | 10.87 | < 0.01 | 9.11 | 37.47 | 13.27 | 50.74 | 41.63 | 9.11 |
| LGSN ₂ | 6.74 | 5.06 | 18 | 7.47 | < 0.01 | 8.44 | 32.21 | 13.51 | 45.72 | 37.28 | 8.44 |
| WA 1 | 5.61 | 8.87 | 9.01 | 4.86 | 8.44 | 9.91 | 19.48 | 27.22 | 46.7 | 36.79 | 9.91 |
| WA ₂ | 4.41 | 6.78 | 10.81 | 4.4 | 8.44 | 9.75 | 19.62 | 24.97 | 44.59 | 34.84 | 9.75 |
| PSL | 6.88 | 5.22 | 13.3 | 7.81 | 9.37 | 9.42 | 27.99 | 24.01 | 52.00 | 42.58 | 9.42 |
| BBL 1 | 8.07 | 7.66 | 23.36 | 10.95 | 12.76 | 16.55 | 42.38 | 36.97 | 79.35 | 62.80 | 16.55 |
| BBL ₂ | 3.84 | 4.16 | 5.62 | < 0.01 | < 0.01 | 13.72 | 9.47 | 17.89 | 27.36 | 13.64 | 13.72 |
| Average | 6.75 | 5.98 | 13.57 | 7.72 | 9.75 | 10.99 | 26.95 | 22.55 | 49.50 | 38.51 | 11.00 |

FIGURE 4. Map of the distribution of REE in the Lenggoksono area (a) element Ce, (b) element Y.

Magnetic Susceptibility

Analysis of magnetic susceptibility tests on 7 samples showed significant variation in the material's magnetic properties. The value of low-frequency magnetic susceptibility (γ_{1f}) ranges from 13.27×10^{-8} m3/kg (BBL 2) up to 4143.47×10^{-8} m3/kg (WA 1), indicating a wide range of magnetic mineral content [24]. The WA 1 sample showed the highest susceptibility, indicating significant concentrations of ferromagnetic minerals. High-frequency vulnerability (γ_{hf}) shows a similar pattern to γ_{lf} , with the lowest value at BBL 2 (12 × 10⁻⁸ m3/kg) and the highest in WA 1 (4137 \times 10⁻⁸ m3/kg). The difference between γ _{If} and γ _{hf} provides information about the presence of very fine superparamagnetic particles, which are generally related to soil formation or weathering processes. Frequency-dependent vulnerability $(\chi_{fd}\%)$ varied from 0.01% (WA 3) to 8.27% (BBL 2). The high χ_{fd} % value of BBL 2 indicates a significant proportion of very fine-sized superparamagnetic particles $($0.03 \mu m$)$, which are often associated with in situ soil formation or intensive weathering processes [25].

| No | Sample Name | χ If $(10^{-8}m^3/kg)$ | χ hf (10 ⁻⁸ m^3 /kg) | χ_{fd} (%) |
|----------------|-------------------|-----------------------------|--|------------------------|
| 1 | LGSN 1 | 346.67 | 345.00 | 0.35 |
| $\overline{2}$ | LGSN ₂ | 661.03 | 659.40 | 0.29 |
| 3 | WA 1 | 4143.47 | 4137.00 | 0.13 |
| $\overline{4}$ | WA 2 | 1015.37 | 1013.40 | 0.16 |
| 5 | PSL | 161.13 | 160.30 | 0.62 |
| 6 | BBL 1 | 1936.23 | 1935.50 | 0.05 |
| | BBL 2 | 13.27 | 12.00 | 8.27 |
| Average | | 1182.45 | 1180.37 | 1.41 |

TABLE 3. Magnetic susceptibility data

Pearson's Correlation

The next part of the study analyzes *Pearson Correlation* between the susceptivity test data, XRF and the OES ICP data. The goal was to find a relationship between two strong or significant variables marked with (*) for a significance of 0.05 and (**) for a significance of 0.01 [26-27]. Using SPSS software, there is an inverse relationship between several pairs indicating that there is a tendency for one variable to act in the opposite direction to another, Al₂O₃ and SiO₂; SO₃ and CuO; Yb₂O₃ and REEmag; γ_{fd} and REEmag with a significance value of 0.05, if the concentration of Al_2O_3 increases, the concentration of SiO_2 tends to decrease. There are also several pairs with a directly proportional or positive relationship showing the relationship between the magnetic properties of an area and the potential presence of minerals containing rare earth elements, namely the elements γ_{lf} and γ_{hf} , Gd; γ_{hf} and Gd; γ_{fd} and Yb_2O_3 ; Nd and LREE, REEmag; Pr and LREE, REEmag; Tb and HREE; Y and SO_3 , REEnonmag; SO_3 and REEnonmag; P_2O_5 and MnO, ZnO ; K_2O and MnO, CuO, ZnO ; Cr_2O_3 and Fe₂O₃, Eu₂O₃; MnO and CuO, ZnO; Fe₂O₃ and Eu₂O₃; LREE dan REEmag; TotalREE and REEmag with a significance of 0.01. The correlation between the element REE and the magnetic susceptibility value of Gadolinium (Gd) and xlf where the correlation between the two is directly proportional. The graph between the correlation between the two is illustrated in FIGURE 5(a) with $R^2 = 0.84$, showing that about 84.09% of the variation in one variable can be explained by the variation in the other variable, indicating a very strong relationship and in FIGURE 5(b) with $R^2 = 0.59$. However, this value is lower compared to FIGURE 5(a), it still shows a significant relationship between the two variables.

FIGURE 5. Correlation graph between (a) γ_{lf} -Gd (b) γ_{lf} -SiO₂

TABLE 4. Pearson Correlation

CONCLUSION

The Lenggoksono region had the highest concentration of $SiO₂$ -dominant compounds in all samples. Neodymium (Nd) shows the most significant REE dominance, with total REE concentrations nearly three times that of the lowest element Terbium (Tb), indicating potential mineralization zones of interest for further exploration. The results of the interpolation mapping show that the element Ce has an even distribution throughout the Lenggoksono region and has the highest concentration at the LGSN 1 point. The magnetic susceptibility of igneous rocks (BBL 2) is lower than that of sand (WA 1). In the Pearson Correlation analysis, several REE elements are significantly correlated with oxide compounds and magnetic susceptibility, indicating the potential use of magnetic susceptibility as an effective and economical proxy in the exploration of critical minerals. The study's results suggest that certain critical minerals can be a marker of other critical minerals, and susceptibility can be used to indicate some critical minerals in natural materials.

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